

$$e) (f \circ g)' = f'g + fg'$$

$$(f(a) \cdot g(a))' = \lim_{h \rightarrow 0} \frac{f(a+h) \cdot g(a+h) - f(a)g(a)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{f(a+h) \cdot g(a+h) + 0 - f(a)g(a)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{f(a+h) \cdot g(a+h) - f(a)g(a+h) + f(a)g(a+h) - f(a)g(a)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{f(a+h) \cdot g(a+h) - f(a)g(a+h) + f(a)g(a+h) - f(a)g(a)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{(f(a+h) - f(a)) \cdot g(a+h) + f(a)(g(a+h) - g(a))}{h}$$

$$= \lim_{h \rightarrow 0} \frac{(f(a+h) - f(a)) \cdot g(a+h)}{h} + \lim_{h \rightarrow 0} \frac{f(a)(g(a+h) - g(a))}{h}$$

$$= \lim_{h \rightarrow 0} \frac{(f(a+h) - f(a))}{h} \cdot \lim_{h \rightarrow 0} g(a+h) + f(a) \lim_{h \rightarrow 0} \frac{g(a+h) - g(a)}{h}$$

$$= f'(a) \cdot g(a) + f(a) \cdot g'(a)$$